

# TEMPLE UNIVERSITY

Department of Mathematics

## Analysis Seminar

Room 617 Wachman Hall

Monday, April 8 2019, 2:40 p.m.

*The Atiyah-Patodi-Singer index on manifolds  
with non-compact boundary*

by Maxim Braverman

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**Abstract:** We study the index of the APS boundary value problem for a strongly Callias-type operator  $D$  on a complete Riemannian manifold  $M$ . We use this index to define the relative eta-invariant of two strongly Callias-type operators  $A$  and  $A'$ , which are equal outside of a compact set. Even though in our situation the  $\eta$ -invariants of  $A$  and  $A'$  are not defined, the relative  $\eta$ -invariant behaves as if it were the difference of the  $\eta$ -invariants of  $A$  and  $A'$ . We also define the spectral flow of a family of such operators and use it to compute the variation of the relative  $\eta$ -invariant. (Joint work with Pengshuai Shi.)