

# On the Regularity of Rectifiable $n$ -Varifolds in the Critical Dimension $n$ .

Jessica Merhej

*Abstract:* The theory of “rectifiability” provides a measure theoretic notion of “smoothness” for surfaces which are not smooth in the usual sense. *Rectifiable varifolds* were introduced as a generalization of minimal surfaces. Existence and regularity of rectifiable varifolds have been a major field of study in Geometric Measure Theory. Allard’s regularity theorem is an outstanding result concerning the regularity of rectifiable varifolds. It examines the important question of how regular will a rectifiable  $n$ -varifold  $M$  be, if we assume bounded and  $L^p$  conditions on the generalized mean curvature of  $M$ , for  $p > n$ .

This talk is concerned with the critical dimension  $n$ . More precisely, how regular will a rectifiable  $n$ -varifold  $M$  be, if we assume bounded and  $L^n$  conditions on the generalized mean curvature of  $M$ .